

# Geometry Control Method of Lusail CP3A Bridge

The background of the slide is a digital rendering of the Lusail CP3A Bridge. The bridge features a prominent, large, blue circular pylon on the left side, from which several cables extend to support the bridge deck. The bridge spans across a body of water. In the background, a dense urban skyline is visible under a twilight sky with soft, warm colors. The overall scene is presented in a cinematic, slightly desaturated style.

Civil Engineering Center  
Dr. Hiroshi TANAKA

# Contents

# Geometry Control ?

- Shape bridge up within geometry allowance of Lusail CP3A
- **Hanger Tension Force : Error < 10%**
- **Very Hard to realize !!**

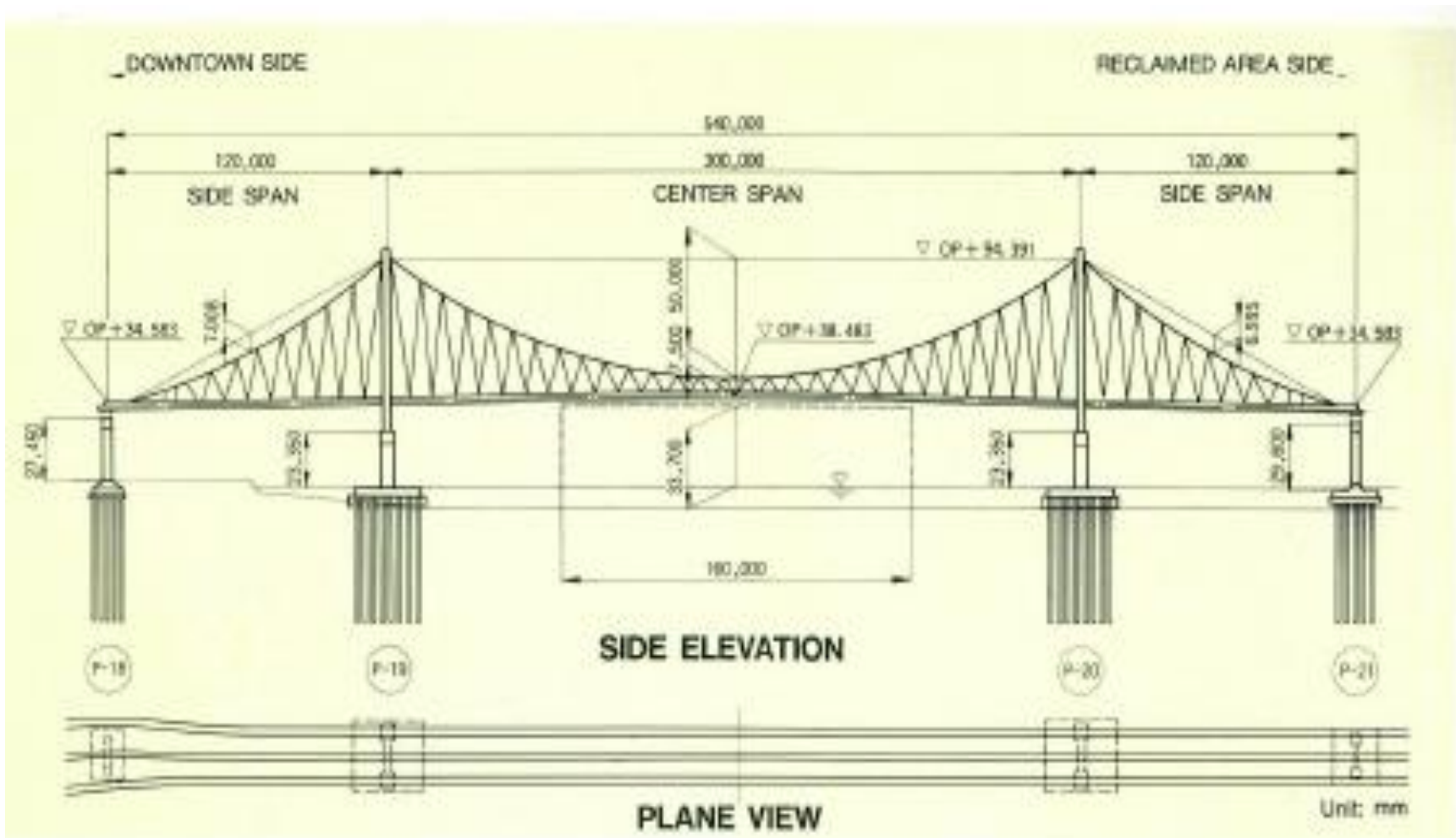
# Konohana Bridge

Self Anchored Suspension Bridge with Inclined hangers



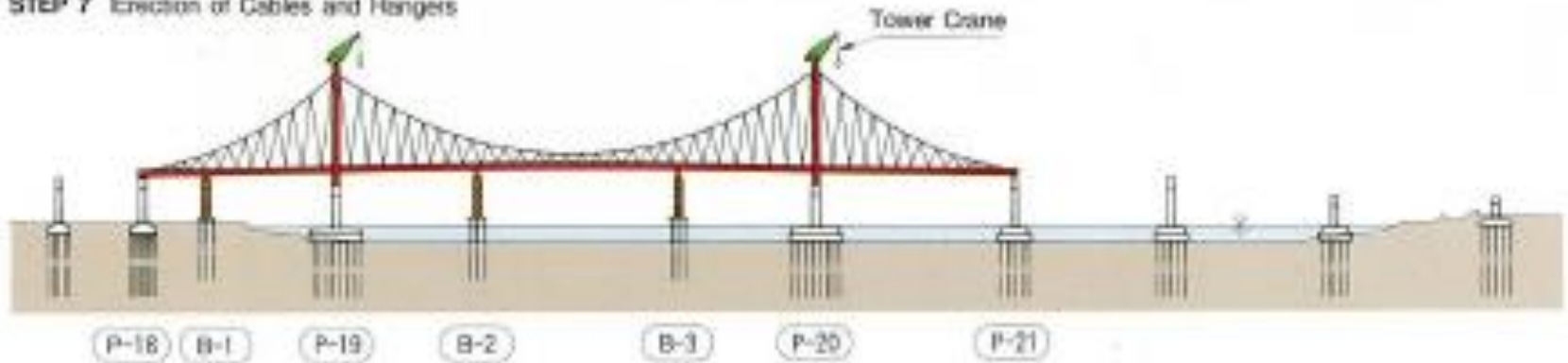
Located in Osaka Japan, 1986

# General View of Konohana Bridge

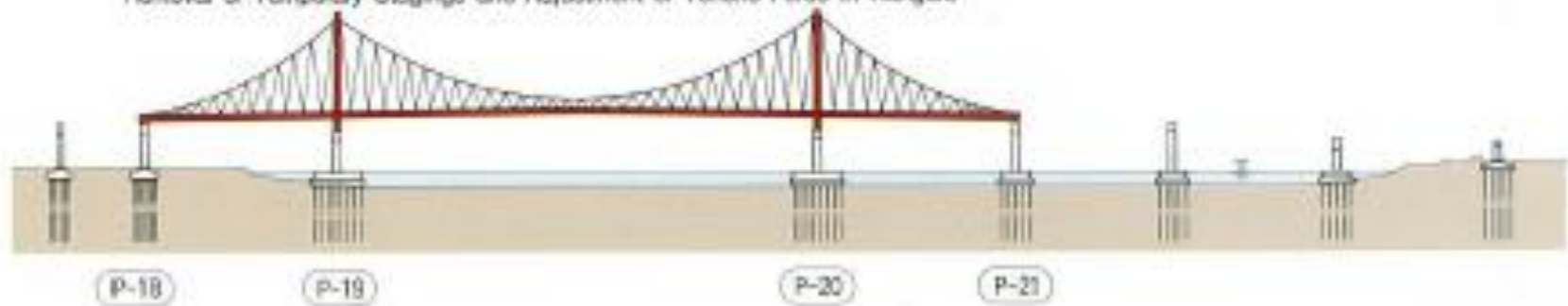


# Bents Removal

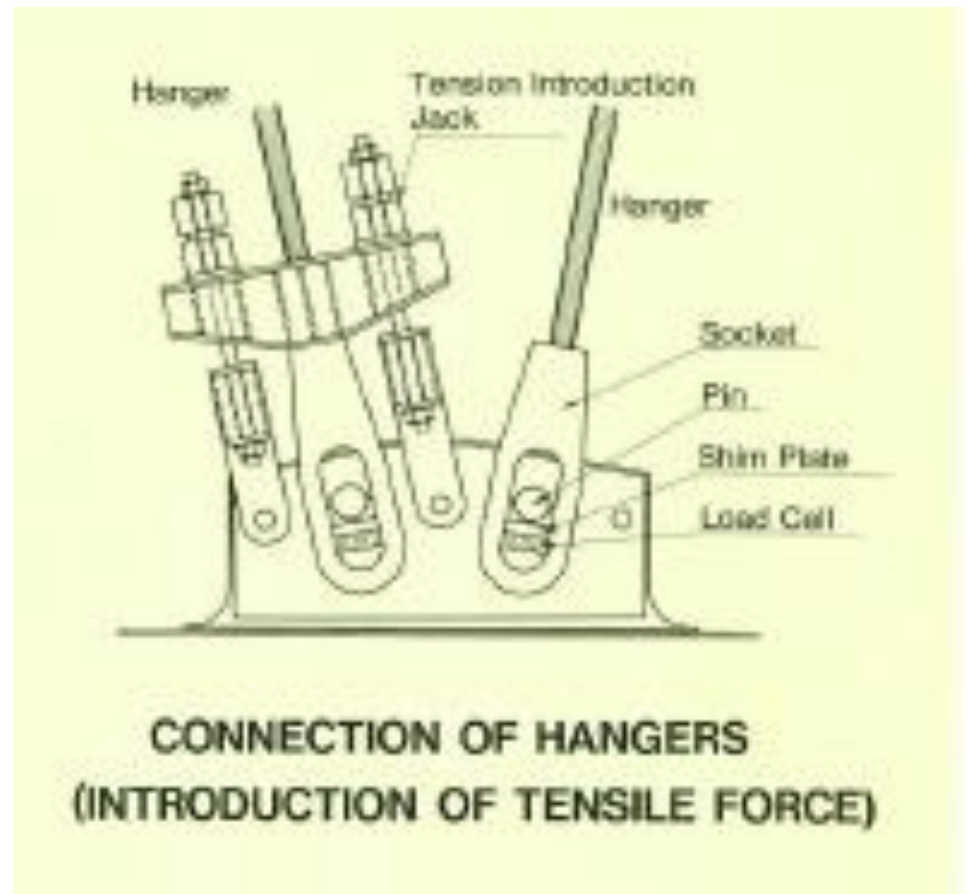
STEP 7 Erection of Cables and Hangers



STEP 8 Jacking down of Main Girder at Temporary Stagings  
Removal of Temporary Stagings and Adjustment of Tensile Force in Hangers



# Hanger Anchor Part

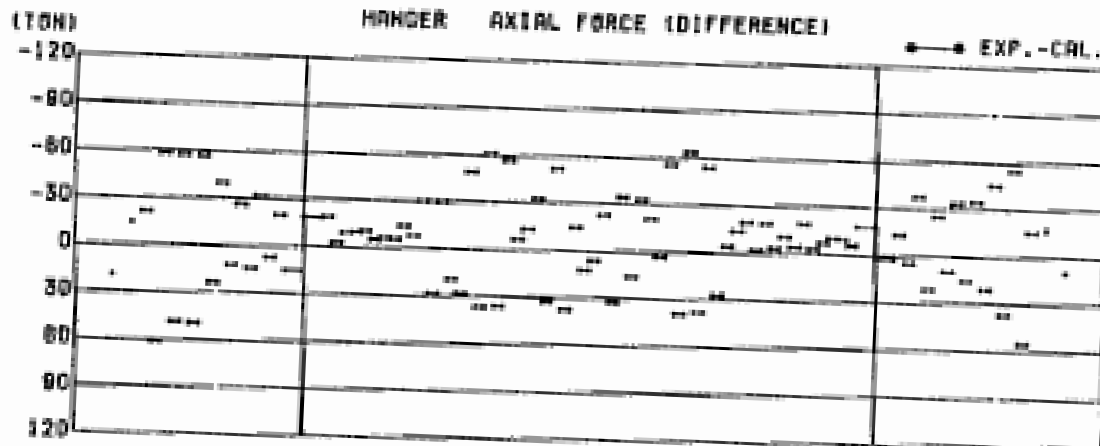
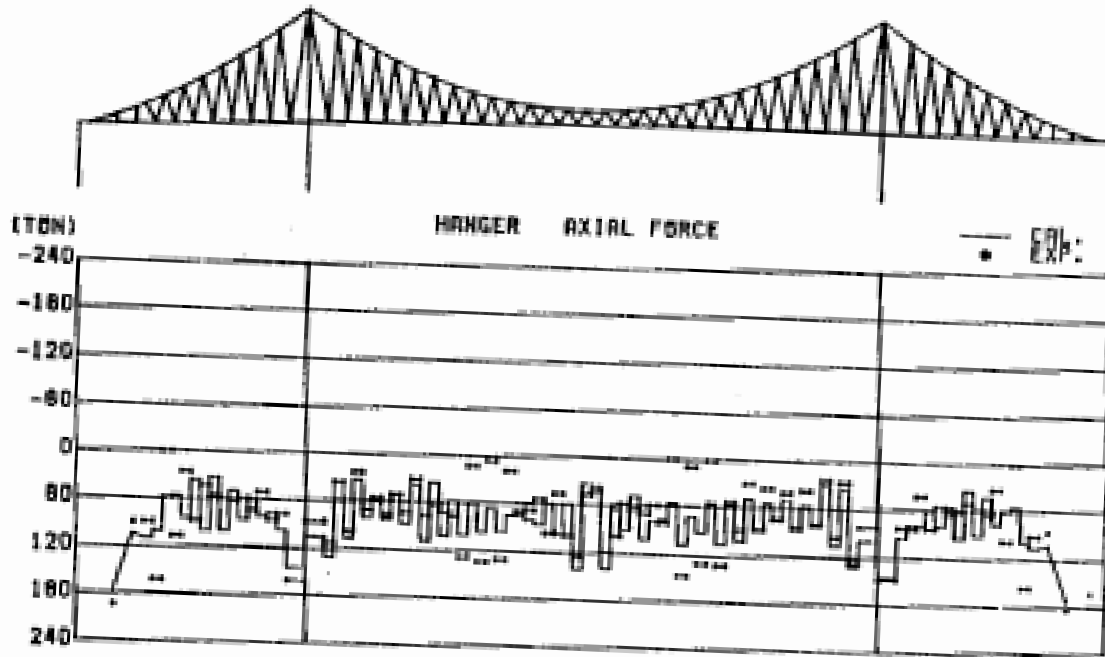


# Cable Tension Adjustment Work at Site

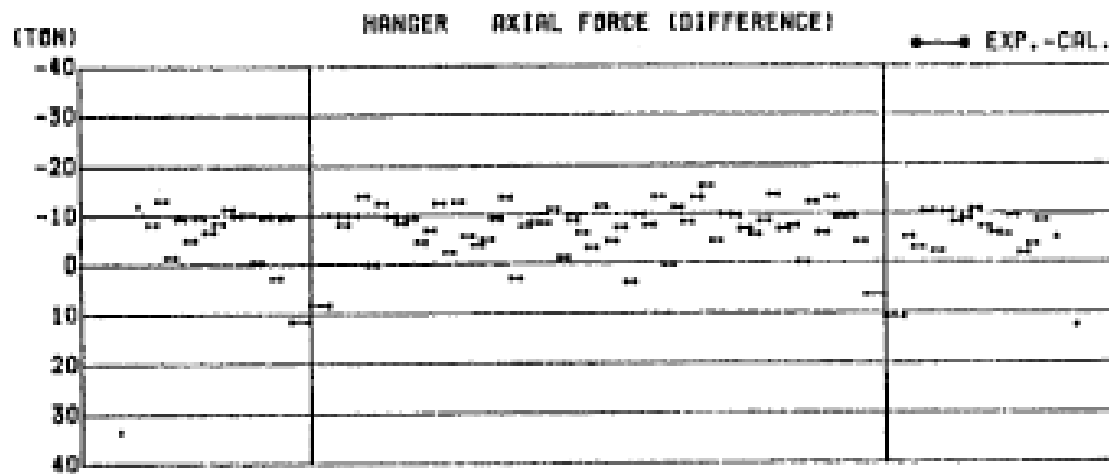
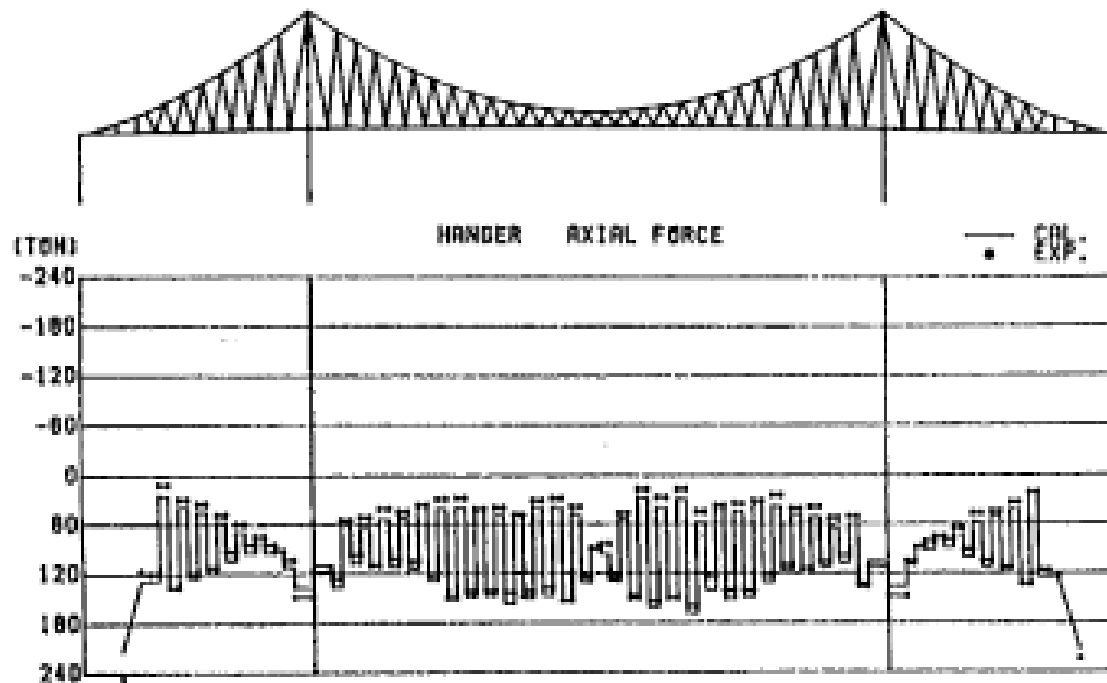




# Hanger Tension Error



Errors are large !



Errors are within allowance!  
 $\pm 20$  ton

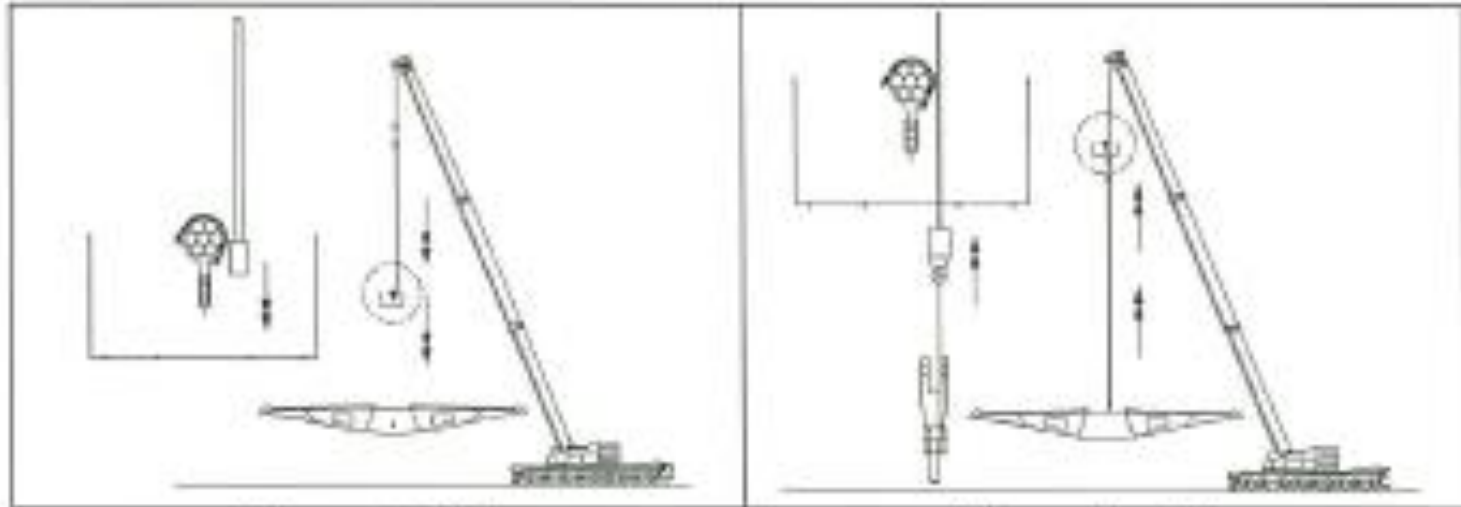
# Main Cable Installation



# Temporary Bents



# Hanger Installation



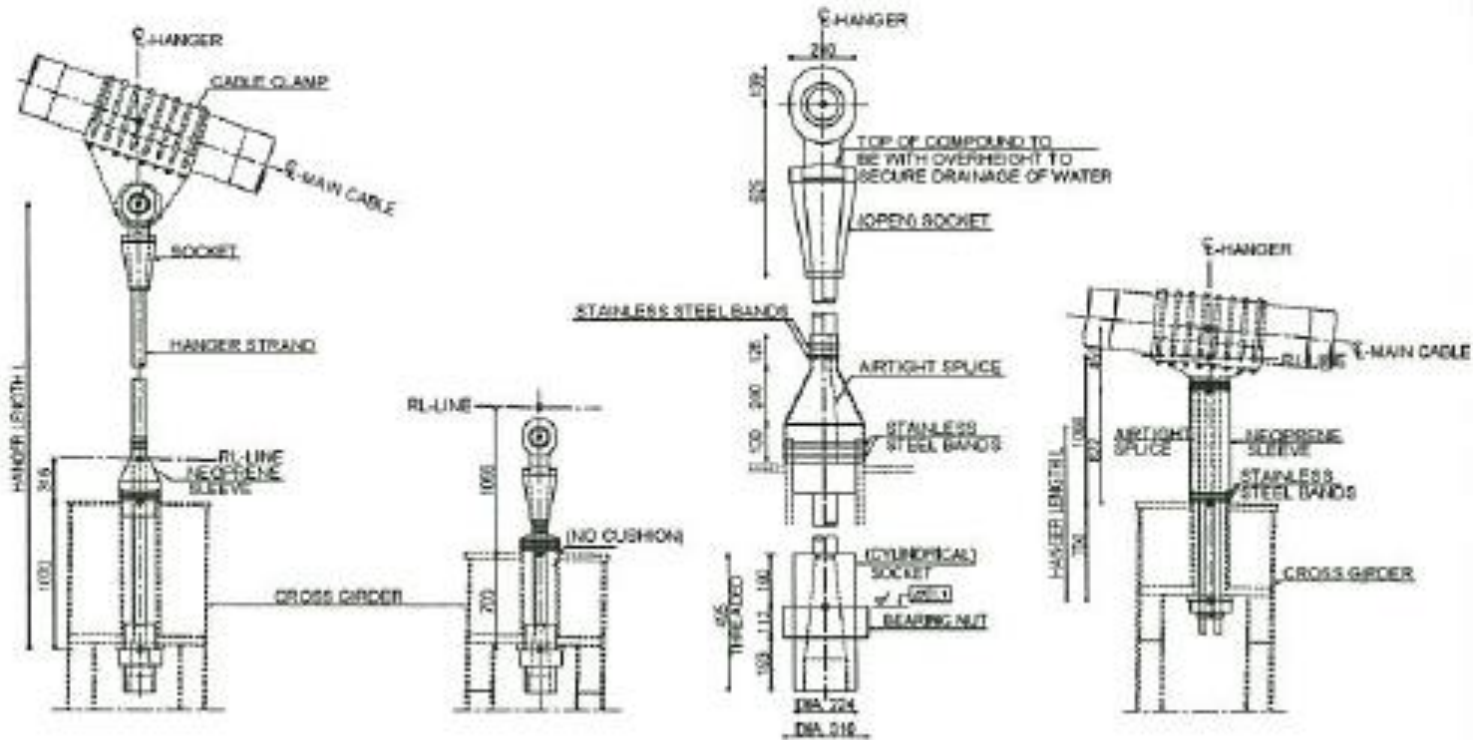
Below about 15m

Above about 15m



Installation of hanger cable in Br 8

# Hanger System



[H1 type]

[H2 type]

# Hanger Tension Adjustment System



Bolt Tensioner Fit up Test



Bolt Tensioner Fit up Test

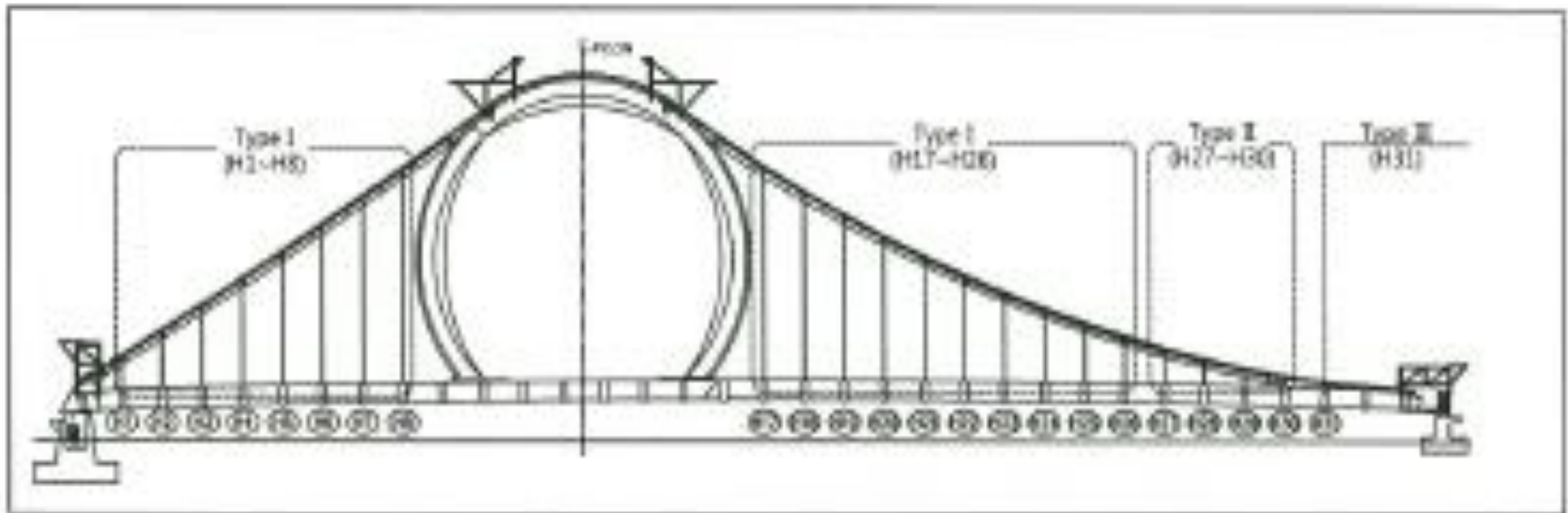


New Tensioner Mock Up



New Tensioner Mock Up

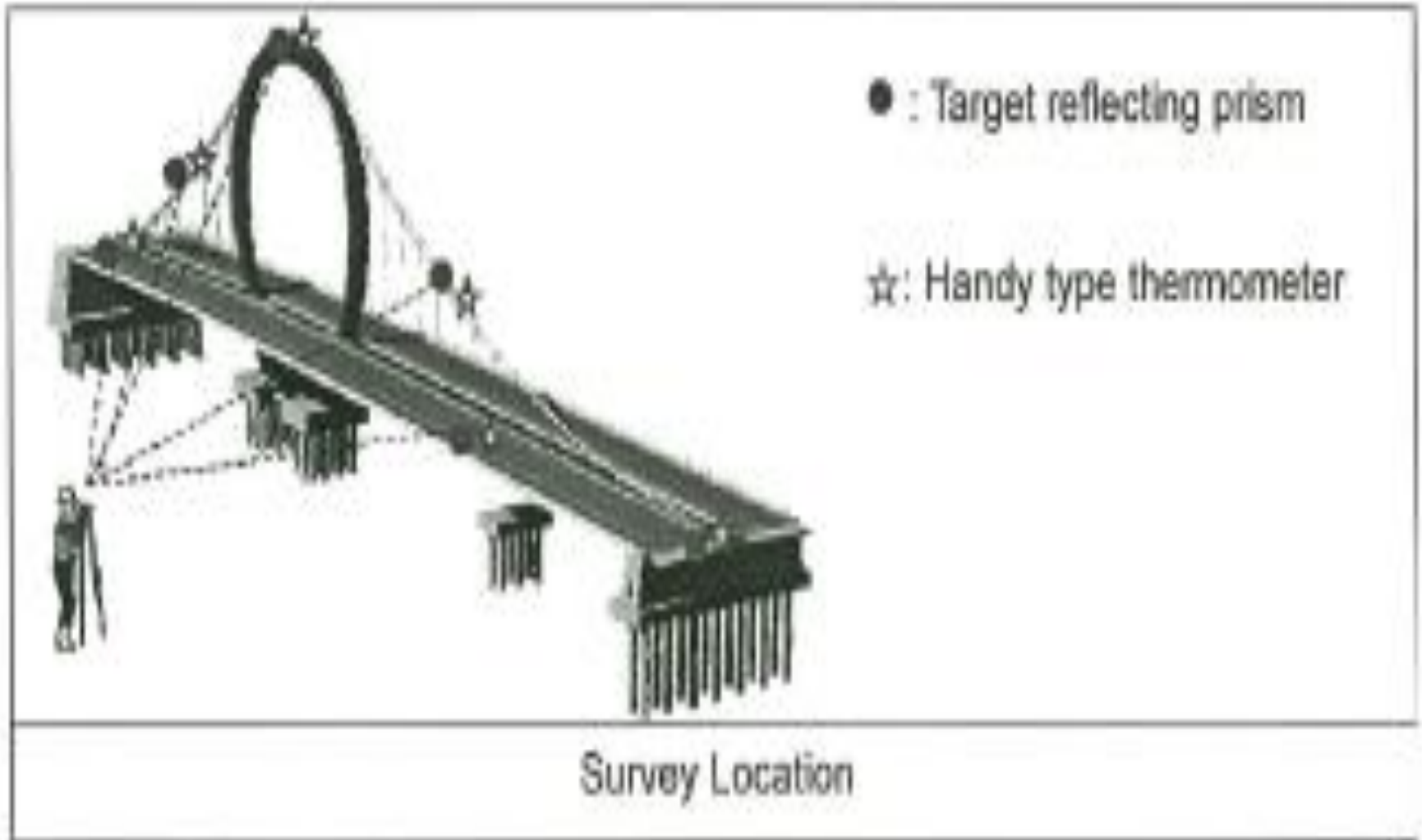
# Bents Removal



Br 8



# Geometry Survey



# Error Factors

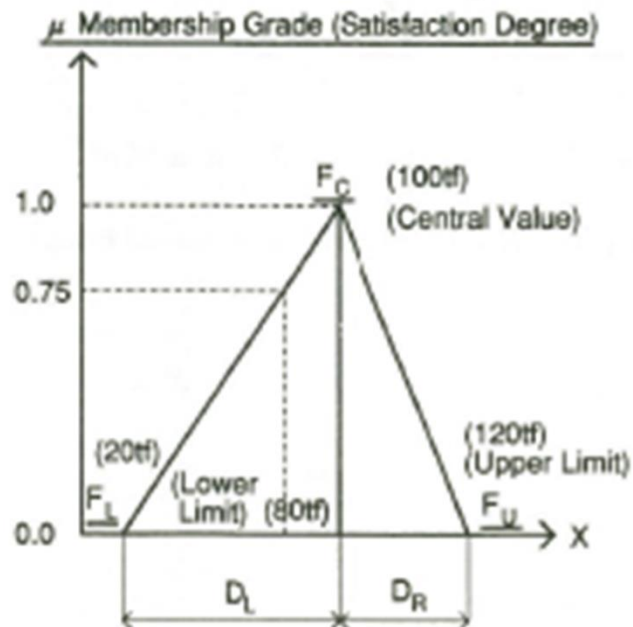
Tolerance Suggestion Value (TSV)

$$= 1.2 \times ( |\Delta_{HT}| + |\Delta_{SW}| + |\Delta_{CE}| + |\Delta_{CF}| + |\Delta_{CR}| ) + \Delta_{EC}$$

Hanger Force( $\Delta_{HT}$ )	Tolerance for hanger force is $\pm 5\%$ (by Particular Technical Specifications GQ626/PTS004/CP3A )
Girder Weight ( $\Delta_{SW}$ )	Tolerance for girder weight including slab weight is $\pm 3\%$ (determined by contractor)
Cable Elasticity( $\Delta_{CE}$ )	Tolerance for modulus of elasticity is 155,000 MPa $\pm$ 8,000 MPa (by Particular Technical Specifications)
Cable Fabrication ( $\Delta_{CF}$ )	Tolerance for cable fabrication is $\Delta L_0 = \pm ( \sqrt{L_0} + 5\text{mm} )$ ; $L_0$ in m (by Particular Technical Specifications)
Cable Creep ( $\Delta_{CR}$ )	0.30 mm/m $\pm$ 0.25 mm/m (by Bridon's experiment result)
Girder Pre-camber ( $\Delta_{EC}$ )	Analysis Gap between GP626/9996/CP3A drawing pre-camber and independent Initial Shape Analysis

# Applied Theory

- Fuzzy satisfaction concept
- Designer's satisfaction → Maximum



# Side Span of Lusail 3CPA Bridge 8

[Lusail BR 8 Side-Span] Hanger Tension Adjustment by Fuzzy Satisfaction Concept - SHEET BY DR. TANAKA -

STEP	15	Description	After Bent Removal
------	----	-------------	--------------------

### Adjusting Shim Thickness [mm]

(+): Shim insertion; (-)Shim removal

Hanger No.	Mem.No.	Amount	Min. Shim	Max. Shim
1	2009	9	-100	100
2	2008	-6	-100	100
3	2007	-8	-100	100
4	2006	0	-100	100
5	2005	8	-100	100
6	2004	-13	-100	100
7	2003	8	-100	100
8	2002	-8	-100	100

### INPUT [KN]

Target (Design Value)	Survey	Allowances	
		(-) %	(+) %
1,707	1,507	-10	10
1,605	1,855	-10	10
1,605	1,795	-10	10
1,605	1,745	-10	10
1,615	1,645	-10	10
1,615	1,815	-10	10
1,625	1,595	-10	10
1,648	1,648	-10	10



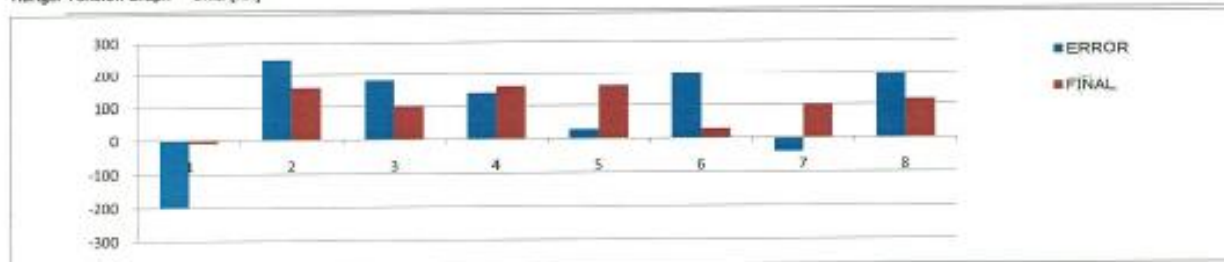
### Shim Adjustment Calculation

Influence Unit: 10 mm

Unit :[KN]

Hanger No.	Influence Matrix								Hanger	Difference (survey-target)	Error Limit		Final Result
	1	2	3	4	5	6	7	8			Lower	Upper	
1	164.522	-62.039	-4.457	0	0	0	0	0	-200	-171	171	-9	
2	-62.039	134.719	-56.635	-5.813	0	0	0	0	250	-161	161	158	
3	-4.457	-56.635	125.143	-50.607	-6.708	0	0	0	180	-161	161	101	
4	0	-5.813	-50.607	116.332	-45.133	-7.296	0	0	140	-161	161	161	
5	0	0	-6.708	-45.133	108.224	-40.205	-7.684	0	30	-162	162	162	
6	0	0	0	-7.296	-40.205	100.729	-35.98	-8.511	200	-162	162	30	
7	0	0	0	0	-7.684	-35.98	93.172	-34.311	-40	-163	163	99	
8	0	0	0	0	0	-8.511	-34.311	79.405	200	-165	165	116	

Hanger Tension Graph Unit: [KN]

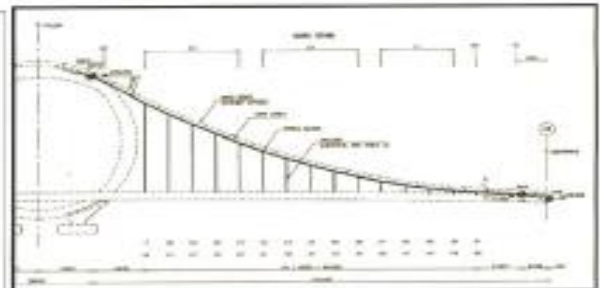
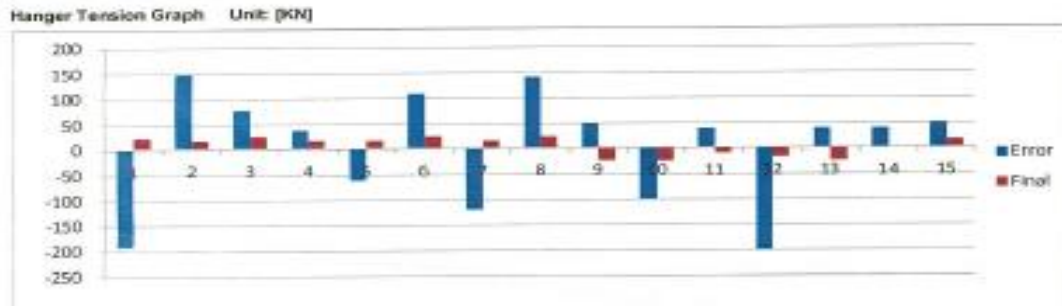


# Center Span of Lusail 3CPA Bridge 8

Adjusting Shim Thickness [mm]				
(+): Shim insertion; (-): Shim removal				
Hanger No.	Mem.No.	Amount	Min.Shim	Max. Shim
17	7102	23	-100	100
18	7103	-10	-100	100
19	7104	-9	-100	100
20	7105	-5	-100	100
21	7106	2	-100	100
22	7107	-6	-100	100
23	7108	4	-100	100
24	7109	-12	-100	100
25	7110	-9	-100	100
28	7111	5	-100	100
27	7112	6	-100	100
28	7113	16	-100	100
29	7114	0	-100	100
30	7115	-6	-100	100
31	7116	-7	-100	100

INPUT [KN]		Allowances						Unit : [KN]			OUTPUT [KN]
Target (Design Val.)	Survey	(-) %	(+) %	(-) [KN]	(+) [KN]	Error(survey-target)	Error Limit		Final Result		
							Lower	Upper			
1,699	1,507	-10	10	-170	170	-192	-170	170	21.7		
1,707	1,855	-10	10	-171	171	148	-171	171	17.0		
1,707	1,785	-10	10	-171	171	78	-171	171	25.0		
1,707	1,745	-10	10	-171	171	38	-171	171	16.7		
1,707	1,645	-10	10	-171	171	-62	-171	171	16.4		
1,706	1,815	-10	10	-171	171	109	-171	171	25.0		
1,706	1,585	-10	10	-171	171	-120	-171	171	16.2		
1,706	1,848	-10	10	-171	171	142	-171	171	24.7		
1,705	1,755	-10	10	-171	171	50	-171	171	-22.8		
1,706	1,805	-10	10	-171	171	-100	-171	171	-23.9		
1,716	1,755	-10	10	-172	172	40	-172	172	-9.5		
1,706	1,505	-10	10	-171	171	-200	-171	171	-17.0		
1,696	1,736	-10	10	-170	170	40	-170	170	-24.5		
1,696	1,736	-10	10	-170	170	40	-170	170	-0.8		
1,706	1,756	-10	10	-171	171	50	-171	171	16.9		

Shim Adjustment Calculation		Influence Unit: 10 mm													
Influence Matrix															
Hanger No.	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31
17	74.114	-33.388	-8.403	-1.443	0	0	0	0	0	0	0	0	0	0	0
18	-33.388	87.979	-33.702	-7.534	0	0	0	0	0	0	0	0	0	0	0
19	-8.403	-33.702	93.884	-36.821	-7.258	0	0	0	0	0	0	0	0	0	0
20	-1.443	-7.534	-36.821	99.279	-40.348	-6.952	0	0	0	0	0	0	0	0	0
21	0	0	-7.258	-40.348	104.627	-43.999	-6.503	0	0	0	0	0	0	0	0
22	0	0	0	-6.952	-43.999	110.046	-47.672	-5.929	0	0	0	0	0	0	0
23	0	0	0	0	-6.503	-47.672	115.644	-51.383	-5.233	0	0	0	0	0	0
24	0	0	0	0	0	-5.929	-51.383	120.773	-55.02	-4.452	0	0	0	0	0
25	0	0	0	0	0	0	-5.233	-55.02	125.891	-68.546	-3.584	0	0	0	0
26	0	0	0	0	0	0	0	-4.452	-68.546	130.735	-61.861	-2.74	0	0	0
27	0	0	0	0	0	0	0	0	-3.584	-61.861	135.1	-84.824	-1.913	0	0
28	0	0	0	0	0	0	0	0	0	-2.74	-84.824	138.948	-87.453	-1.184	0
29	0	0	0	0	0	0	0	0	0	0	-1.913	-87.453	142.16	-69.556	0
30	0	0	0	0	0	0	0	0	0	0	0	-1.184	-69.556	144.957	-72.064
31	0	0	0	0	0	0	0	0	0	0	0	0	0	-72.064	111.638



# INPUT & OUTPUT (1)

STEP	15	Description	After Bent Removal
------	----	-------------	--------------------

Adjusting Shim Thickness [mm]				
(+): Shim insertion; (-)Shim removal				
Hanger No.	Mem.No.	Amount	Min.Shim	Max. Shim
17	7102	23	-100	100
18	7103	-10	-100	100
19	7104	-9	-100	100
20	7105	-5	-100	100
21	7106	2	-100	100
22	7107	-6	-100	100
23	7108	4	-100	100
24	7109	-12	-100	100
25	7110	-9	-100	100
26	7111	5	-100	100
27	7112	6	-100	100
28	7113	18	-100	100
29	7114	0	-100	100
30	7115	-6	-100	100
31	7116	-7	-100	100

INPUT [KN]		Unit :[KN]								OUTPUT [KN]
Target (Design Val.	Survey	Allowances				Error(survey -target)	Error Limit		Final Result	
		(-) %	(+) %	(-) [KN]	(+) [KN]		Lower	Upper		
1,689	1,507	-10	10	-170	170	-192	-170	170	21.7	
1,707	1,855	-10	10	-171	171	148	-171	171	17.0	
1,707	1,785	-10	10	-171	171	78	-171	171	25.0	
1,707	1,745	-10	10	-171	171	38	-171	171	16.7	
1,707	1,645	-10	10	-171	171	-62	-171	171	16.4	
1,706	1,815	-10	10	-171	171	109	-171	171	25.0	
1,705	1,585	-10	10	-171	171	-120	-171	171	16.2	
1,706	1,848	-10	10	-171	171	142	-171	171	24.7	
1,705	1,755	-10	10	-171	171	50	-171	171	-22.8	
1,706	1,606	-10	10	-171	171	-100	-171	171	-23.9	
1,716	1,756	-10	10	-172	172	40	-172	172	-9.5	
1,705	1,505	-10	10	-171	171	-200	-171	171	-17.0	
1,698	1,736	-10	10	-170	170	40	-170	170	-24.5	
1,696	1,736	-10	10	-170	170	40	-170	170	-0.8	
1,706	1,756	-10	10	-171	171	50	-171	171	16.9	

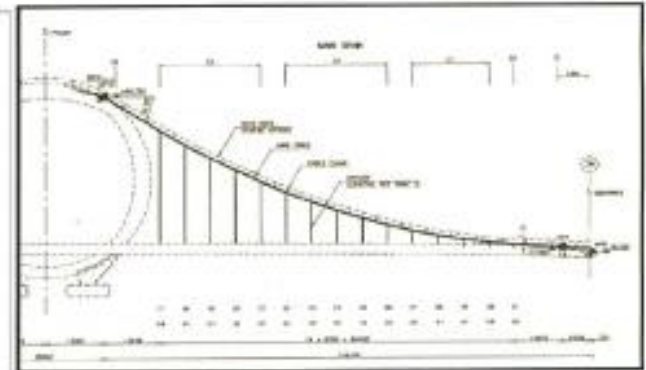
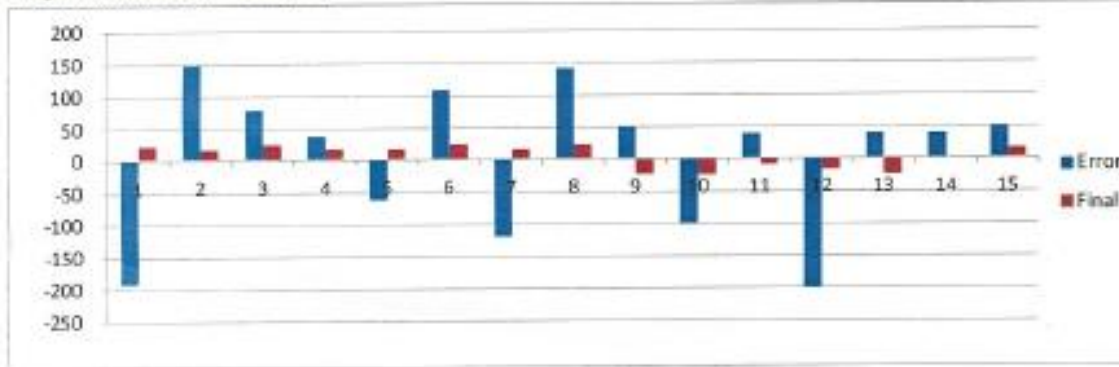
# INPUT & OUTPUT (2)

Shim Adjustment Calculation		Influence Unit: 10 mm													
Influence Matrix															
Hanger No	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31
17	74.114	-33.368	-8.405	-1.443	0	0	0	0	0	0	0	0	0	0	0
18	-33.368	87.979	-33.702	-7.534	0	0	0	0	0	0	0	0	0	0	0
19	-8.405	-33.702	93.884	-36.821	-7.258	0	0	0	0	0	0	0	0	0	0
20	-1.443	-7.534	-36.821	99.279	-40.348	-6.952	0	0	0	0	0	0	0	0	0
21	0	0	-7.258	-40.348	104.627	-43.969	-6.503	0	0	0	0	0	0	0	0
22	0	0	0	-6.952	-43.969	110.048	-47.672	-5.929	0	0	0	0	0	0	0
23	0	0	0	0	-6.503	-47.672	113.444	-51.363	-5.233	0	0	0	0	0	0
24	0	0	0	0	0	-5.929	-51.363	120.773	-55.02	-4.452	0	0	0	0	0
25	0	0	0	0	0	0	-5.233	-55.02	125.891	-58.548	-3.584	0	0	0	0
26	0	0	0	0	0	0	0	-4.452	-58.548	130.735	-61.861	-2.74	0	0	0
27	0	0	0	0	0	0	0	0	-3.584	-61.861	135.1	-64.824	-1.913	0	0
28	0	0	0	0	0	0	0	0	0	-2.74	-64.824	138.948	-67.453	-1.164	0
29	0	0	0	0	0	0	0	0	0	0	-1.913	-67.453	142.16	-69.558	0
30	0	0	0	0	0	0	0	0	0	0	0	-1.164	-69.558	144.957	-72.094
31	0	0	0	0	0	0	0	0	0	0	0	0	0	-72.094	111.638

**N.B. ) Precise Influence Matrix is necessary**

# INPUT & OUTPUT (3)

Hanger Tension Graph Unit: [KN]





# Difference between self-anchored suspension bridges and cable stay bridges

- Hangers of self-anchored suspension bridges can not control erection errors of decks and towers .

Therefore erection of decks and towers should be done carefully.

# Conclusions

- Cable tension adjustment is vital for cable suspended bridges.
- Lusail CP3A bridges also needs this system.
- We can realize precise construction by this system.
- Applying this software we can save time and money.

We sincerely hope perfect construction of Lusail CP3A.  
Then Samsung can receive client's highest evaluation.

# Appendix      Used Basic Theory

**IEEE COMPUTER SOCIETY  
PRESS REPRINT**

## **OPTIMUM CABLE TENSION ADJUSTMENT USING FUZZY MATHEMATICAL PROGRAMMING**

**Hitoshi Furuta, Masashiro Kamei, Masakatsu Kaneyoshi,  
and Hiroshi Tanaka**

**Second International Symposium on Uncertainty  
Modeling and Analysis**

University of Maryland  
College Park, Maryland  
April 25-28, 1993

Sponsored by the  
IEEE Computer Society  
Technical Committee on Computer Graphics  
in cooperation with  
ACM/SIGGRAPH

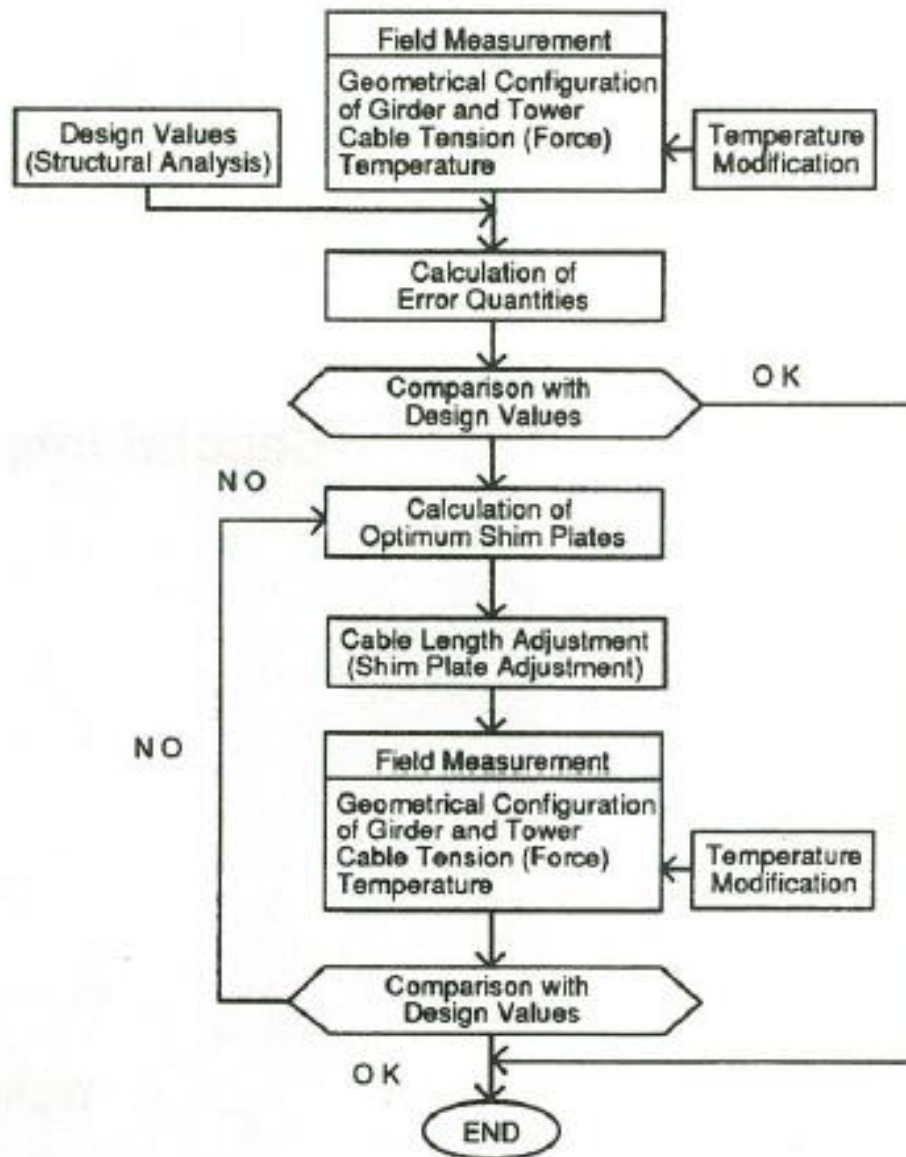
## 1: Introduction

To determine the optimum cable prestresses in the design of cable-stayed bridges is one of the most important, but time consuming procedure. However, various kinds of errors will be introduced during fabrication or construction (see Fig. 1)<sup>1)</sup>. Therefore, cable length adjustment is necessary to alter the stress distribution and the geometrical configuration of the bridge at the construction site. The authors have developed a method to overcome these problems with the aid of the fuzzy regression analysis<sup>2)</sup>. Through several applications in the design and construction of actual cable-stayed bridges, it has been proved that the method is not only simple to handle, but also very practical for the design and construction of cable-stayed bridges.

In this paper, an attempt is made to improve the method by introducing the concept of "satisfaction". The degree of satisfaction is defined in such a way that when the aspire of a designer is completely achieved, the satisfaction degree is one, and when the aspire is not achieved at all, the satisfaction degree is zero. Evidently,

## 2: Concept of satisfaction

The most prominent characteristic of a cable-stayed bridge is the introduction of cable prestresses to change the static equilibrium in order to reduce its weight. However, the optimum state of cable prestresses should be determined from various points of view. As well as the weight reduction, easiness of fabrication and construction should be considered. Moreover, various kinds of errors can not be avoided so that the introduction of engineer's knowledge and experience is desirable to derive a practically feasible solution for the determination of cable prestresses. Based upon engineering judgment of a designer, a certain desirable range is first given for each force of structural member. Especially, experienced engineers may provide appropriate desirable ranges with the most desirable values. This desirable range is interpreted in terms of fuzzy sets defined by membership functions<sup>4)</sup>. An example of desirable range is presented in Fig. 2, in which  $F_C$  is the most desirable value and the values less than  $F_L$  and larger than  $F_U$  are not accepted. Then, the membership grade corresponds to the degree of satisfaction; 1, 0, and 0 are the degrees of satisfaction for  $F_C$ ,  $F_L$ , and  $F_U$ , respectively. Experienced engineers tend to give an  $F_C$  value closer to  $F_U$ . In this example,  $F_U$ ,  $F_L$ , and  $F_C$  are 120 tf, 20 tf, and 100 tf. In this case, it can be said that the designer requires about 100 tf for the prestress of the cable. When 80 tf is obtained as a cable prestress, the degree of satisfaction is calculated as 0.75 from the membership function shown in Fig. 2.



**Fig.1 Management of Erection Accuracy of Cable-Stayed Bridge**

### 3: Determination of optimum cable prestress using fuzzy mathematical programming

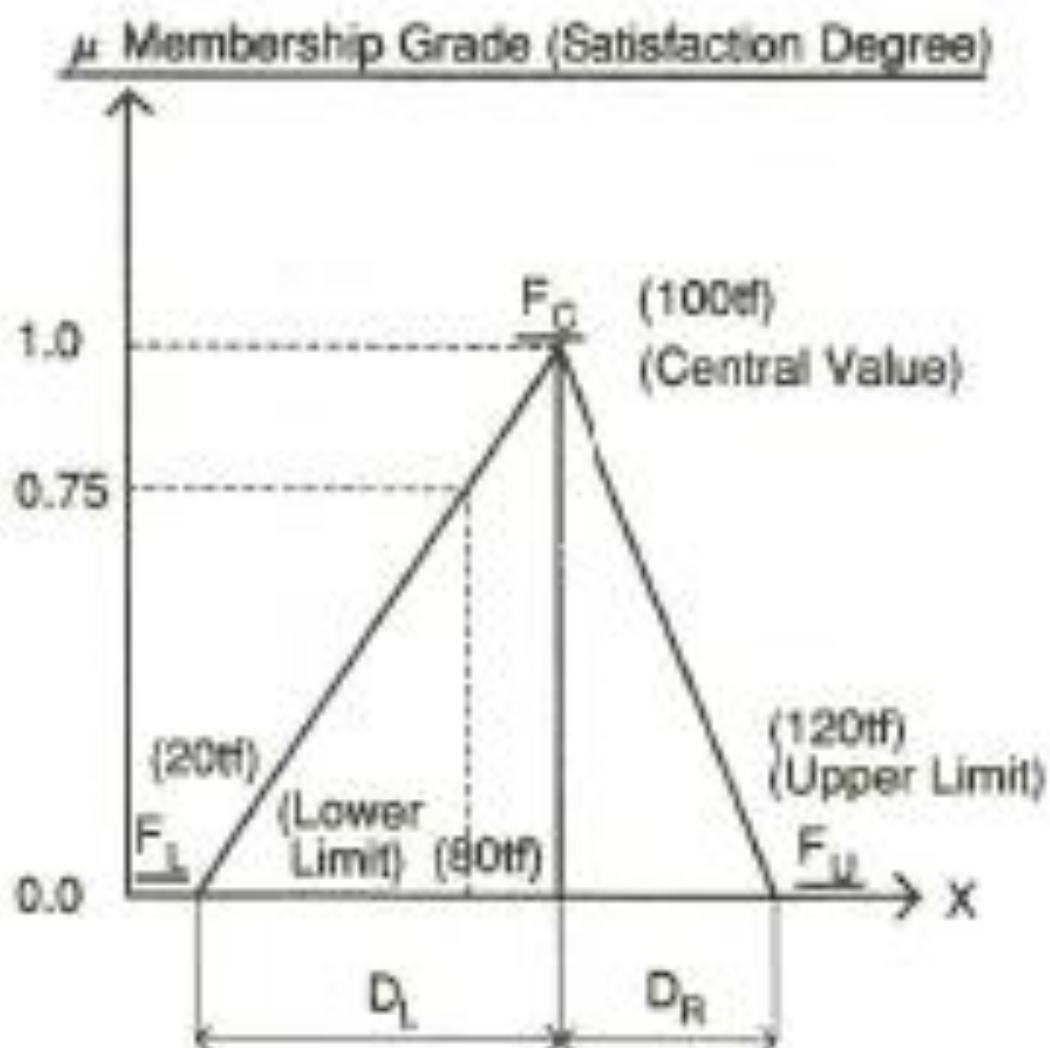
Assuming that the required prestresses are given in terms of fuzzy sets, the problem treated here results in

$$F_{0i} = \tilde{F}_{0i} \quad (i=1, \dots, M) \quad \dots\dots\dots (1)$$

where  $\tilde{F}_0$  is the desirable structural member force specified by a fuzzy set. The wave symbol (i.e.,  $\sim$ ) indicates fuzzy quantities.  $M$  is the number of member forces. Structural member forces after introducing prestresses,  $F_{0i}$ , are calculated as follows:

$$F_0 = F_d + \sum_{j=1}^N X_j K_{ji} \quad \dots\dots\dots (2)$$

where  $F_d$  is structural member force due to dead load,  $X_j$  is a variable representing cable prestress, and  $K_{ji}$  is member force influence coefficient by unit prestress of the cable.  $N$  is the number of cables. Fig. 3 shows the flow diagram of structural analysis for cable-stayed bridges.





Paying attention to the  $j$ -th member force, the following equation is derived from Eqs. 1 and 2.

$$F_{Lj} - F_{dj} \leq \sum_{j=1}^N X_i K_{ji} \leq F_{Uj} - F_{dj} \quad \dots\dots\dots (3)$$

Using the following transformations

$$F_{Lj}' = F_{Lj} - F_{dj} \quad \dots\dots\dots (4)$$

$$F_{Uj}' = F_{Uj} - F_{dj} \quad \dots\dots\dots (5)$$

the degrees of satisfaction are expressed as follows, for the left-hand side and right-hand side of the central value of the membership function.

For left-hand side

$$\mu_{jL}(u) = \begin{cases} 0.0 & (u \leq F_{Lj}') \\ 1.0 - (F_{Cj}' - \sum_{j=1}^N X_i K_{ji}) / D_{Lj} & (F_{Lj}' \leq u \leq F_{Cj}') \end{cases} \quad \dots\dots\dots (6)$$

For right-hand side

$$\mu_{jR}(u) = \begin{cases} 1.0 - (F_{Cj}' - \sum_{j=1}^N X_i K_{ji}) / D_{Rj} & (F_{Lj}' \leq u \leq F_{Uj}') \\ 0.0 & (u \leq F_{Uj}') \end{cases} \quad \dots\dots\dots (7)$$

where  $D_{Rj}$  and  $D_{Lj}$  denote the scatter parameters of right-

hand and left-hand sides, respectively.

Here, two kinds of objective functions are employed:

$$\text{Objective function 1: } \mu_D(u) = \max \{ \min (\mu_{1L}(u), \mu_{1R}(u), \dots, \mu_{mL}(u), \mu_{mR}(u)) \dots \dots \dots (8)$$

$$\text{Objective function 2: } \mu_D(u) = \sum_{j=1}^M \mu_j(u) \rightarrow \max \dots \dots (9)$$

The above fuzzy mathematical programming problem consisting of Eqs. 7 (constraints) and 8 or 9 (objective function) can be solved by using a linear programming computer package without difficulty. The problem with Eq. 8 as the objective function is referred to Method 1, whereas the problem with Eq. 9 is referred to Method 2.